

P. 1045
 #3, 11, 15, 41, 49,
 50, 59
 11.5A

$$3.) (-3+2i) - (4-4i)$$

$$-3+2i-4+4i$$

$$\boxed{-7+6i}$$

$$11.) (3-4i)(2+i)$$

$$6+3i-8i-4i^2$$

$$6-5i-4(-1)$$

$$6-5i+4$$

$$\boxed{10-5i}$$

$$15.) \frac{10}{3-4i} \frac{3+4i}{3+4i}$$

$$\frac{30+40i}{9+12i-12i-4i^2}$$

$$\frac{30+40i}{9-16(-1)}$$

$$\frac{30+40i}{25}$$

$$\frac{30}{25} + \frac{40i}{25}$$

$$\boxed{\frac{6}{5} + \frac{8i}{5}}$$

$$41.) \sqrt{-25} = \boxed{5i}$$

$$49.) x^2 - 6x + 13 = 0$$

CANNOT BE FACTORED

$$\frac{+6 \pm \sqrt{(-6)^2 - 4(13)}}{2}$$

$$\frac{+6 \pm \sqrt{36-52}}{2}$$

$$\frac{6 \pm \sqrt{-16}}{2}$$

$$\frac{6 \pm 4i}{2}$$

$$\boxed{3+2i, 3-2i}$$

$$50.) x^2 + 4x + 8 = 0$$

$$\frac{-4 \pm \sqrt{4^2 - 4(8)}}{2}$$

$$\frac{-4 \pm \sqrt{16-32}}{2}$$

$$\frac{-4 \pm \sqrt{-16}}{2}$$

$$\frac{-4 \pm 4i}{2}$$

$$\boxed{-2+2i, -2-2i}$$

$$59.) x^3 - 8 = 0$$

$$x^3 = 8$$

$$x = 2$$

But there are 2
 complex solutions -
 must be 3 total!

Factor: $(x-2)(x^2+2x+4) = 0$

$$x-2=0 \quad x^2+2x+4=0$$

$$\boxed{x=2}$$

↑
 Real

$$\frac{-2 \pm \sqrt{4-4(4)}}{2}$$

$$\frac{-2 \pm \sqrt{-12}}{2}$$

$$\frac{-2 \pm \sqrt{4} \sqrt{-3}}{2}$$

$$\frac{-2 \pm 2\sqrt{3}\sqrt{-1}}{2}$$

$$\frac{-2 \pm 2\sqrt{3}i}{2}$$

$$\boxed{-1+\sqrt{3}i, -1-\sqrt{3}i}$$

$x-c$ a factor?

4) $4x^4 - 15x^2 - 4 \quad c=2$

$f(2) = 4(2)^4 - 15(2)^2 - 4$
 $64 - 60 - 4 = 0$

$x-2$ is a factor.

$$\begin{array}{r} 2 \overline{) 40 - 150 - 4} \\ \underline{8 \quad 16 \quad 2 \quad 4} \\ 4 \quad 8 \quad 1 \quad 2 \quad 10 \end{array}$$

$(x-2)(4x^3 + 8x^2 + x + 2)$

or
 $(x-2)(4x^2(x+2) + x+2)$
 $(x-2)(x+2)(4x^2+1)$

6) $f(x) = 2x^6 - 18x^4 + x^2 - 9 \quad c=-3$

$f(-3) = 2(-3)^6 - 18(-3)^4 + (-3)^2 - 9$
 $1458 - 1458 + 9 - 9 = 0$

$x+3$ is a factor

$$\begin{array}{r} -3 \overline{) 20 - 180 \quad 1 \quad 0 \quad -9} \\ \underline{-6 \quad 18 \quad 0 \quad 0 \quad -3 \quad 9} \\ 2 \quad -6 \quad 0 \quad 0 \quad 1 \quad -3 \quad 10 \end{array}$$

$(x+3)(2x^5 - 6x^4 + x - 3)$

or
 $(x+3)(2x^4(x-3) + x-3)$
 $(x+3)(x-3)(2x^4+1)$

8) $f(x) = x^6 - 16x^4 + x^2 - 16 \quad c=-4$

$f(-4) = (-4)^6 - 16(-4)^4 + (-4)^2 - 16$
 $= 4096 - 4096 + 16 - 16 = 0$

$x+4$ is a factor

$$\begin{array}{r} -4 \overline{) 1 \quad 0 \quad -16 \quad 0 \quad 1 \quad 0 \quad -16} \\ \underline{-4 \quad 16 \quad 0 \quad 0 \quad -4 \quad 16} \\ 1 \quad -4 \quad 0 \quad 0 \quad 1 \quad -4 \quad 10 \end{array}$$

$(x+4)(x^5 - 4x^4 + x - 4)$

or
 $(x+4)(x^4(x-4) + x-4)$
 $(x+4)(x-4)(x^4+1)$

10) $f(x) = 3x^4 + x^3 - 3x + 1 \quad c = -\frac{1}{3}$
 $f(-\frac{1}{3}) = 3(-\frac{1}{3})^4 + (-\frac{1}{3})^3 - 3(-\frac{1}{3}) + 1$
 $= \frac{1}{27} + -\frac{1}{27} + 3 + 1 = 4$

$x + \frac{1}{3}$ is not a factor.

64) $f(x) = x^4 + 8x^3 - x^2 + 2 \quad [-1, 0]$ ZERO IN INTERVAL?

$f(-1) = (-1)^4 + 8(-1)^3 - (-1)^2 + 2 = 1 - 8 - 1 + 2 = -6$

$f(0) = 0^4 + 8(0)^3 - 0^2 + 2 = 2$

SIGN CHANGE ZERO IN INTERVAL

$x = -.60$

66) $f(x) = 3x^3 - 10x + 9 \quad [-3, 2]$

$f(-3) = 3(-3)^3 - 10(-3) + 9$
 $= -81 + 30 + 9 = -42$

$f(2) = 3(2)^3 - 10(2) + 9$
 $= 16 - 20 + 9 = 5$

SIGN CHANGE - ZERO IN INTERVAL $x = -2.17$

68) $f(x) = x^5 - 3x^4 - 2x^3 + 6x^2 + x + 2 \quad [1.7, 1.8]$

$f(1.7) = (1.7)^5 - 3(1.7)^4 - 2(1.7)^3 + 6(1.7)^2 + 1.7 + 2 = -.35627$

$f(1.8) = (1.8)^5 - 3(1.8)^4 - 2(1.8)^3 + 6(1.8)^2 + 1.8 + 2 = -1.02112$

SIGN CHANGE - ZERO ON INTERVAL $x = 1.73$

FIND REMAINING ZEROS

8) DEGREE 4 ZEROS: $2-i, -i$ $2+i, i$

10) DEGREE 6 ZEROS: $i, 3-2i, -2+i$ $-i, 3+2i, -2-i$

78) Find length of cube if volume is doubled by adding 6 to one edge, 12 to another and subtracting 4 from 3rd.

$V = x^3$
 $2V = 2x^3$
 $2x^3 = (x+6)(x+12)(x-4)$
 $2x^3 = (x^2 + 18x + 72)(x-4)$
 $2x^3 = x^3 + 18x^2 + 72x - 4x^2 - 72x - 288$
 $2x^3 = x^3 + 14x^2 - 288$
 $x^3 - 14x^2 + 288 = 0$
 $x = -4 \quad x = 6$

Form a Polynomial:

11.) DEGREE 4 ZEROS: $3+2i, 4$ -mult 2

$(x-4)^2(x-(3+2i))(x-(3-2i))$
 $(x^2 - 8x + 16)(x-3-2i)(x-3+2i)$
 $(x^2 - 8x + 16)(x^2 - 3x + 2ix - 3x + 9 - 6i - 2ix + 6i - 4i^2)$
 $(x^2 - 8x + 16)(x^2 - 6x + 9 - 4(-1))$
 $(x^2 - 8x + 16)(x^2 - 6x + 13)$
 $x^4 - 6x^3 + 13x^2 - 8x^3 + 48x^2 - 104x + 16x^2 - 96x + 208$
 $x^4 - 14x^3 + 77x^2 - 200x + 208$

12) DEGREE 4 ZEROS: $i, 1+2i$

$$\begin{aligned} & (x-i)(x+i)(x-(1+2i))(x-(1-2i)) \\ & (x^2-i^2)(x^2-2(1)(x)+1^2+2^2) \\ & (x^2+1)(x^2-2x+5) \\ & x^4-2x^3+5x^2+x^2-2x+5 \\ & \boxed{x^4-2x^3+6x^2-2x+5} \end{aligned}$$

13) DEGREE 5 ZEROS $2, -i, 1+i$

$$\begin{aligned} & (x-2)(x-i)(x+i)(x-(1+i))(x-(1-i)) \\ & (x-2)(x^2+1)(x^2-2(1)x+1^2+1^2) \\ & (x^3+x-2x^2-2)(x^2-2x+2) \\ & (x^3-2x^2+x-2)(x^2-2x+2) \\ & x^5-2x^4+2x^3-2x^4+4x^3-4x^2+x^3-2x^2+2x-2x+4x-4 \\ & \boxed{x^5-4x^4+7x^3-8x^2+6x-4} \end{aligned}$$

11) $f(x) = x^3 - 8x^2 + 25x - 26$

From graph $x=2$ is a zero, so divide by $(x-2)$

$$\begin{array}{r|rrrr} 2 & 1 & -8 & 25 & -26 \\ & & 2 & -12 & 26 \\ \hline & 1 & -6 & 13 & 0 \end{array}$$

$x^2 - 6x + 13$, so:

$(x-2)(x^2-6x+13)$ ← Cannot be factored but must have 2 more zeros.

$$\frac{6 \pm \sqrt{(-6)^2 - 4(13)}}{2}$$

$$\frac{6 \pm \sqrt{36 - 52}}{2} = \frac{6 \pm \sqrt{-16}}{2}$$

$$= \frac{6 \pm 4i}{2} = 3 \pm 2i$$

ZEROS: $\boxed{3+2i, 3-2i}$ (COMPLEX) $\boxed{2}$ (REAL)

31) $f(x) = x^4 + 2x^3 + 22x^2 + 50x - 75$
 4 ZEROS - 2 REAL ($x = -3, x = 1$) REAL
 2 COMPLEX

$$\begin{aligned} & (x+3)(x-1) \quad x^2+25 \\ & x^2+2x-3 \quad \begin{array}{l} x^4+2x^3+22x^2+50x-75 \\ -x^4+2x^3-3x^2 \\ \hline 25x^2+50x-75 \\ -25x^2+50x-75 \\ \hline 0 \end{array} \end{aligned}$$

$$\begin{aligned} x^2+25 &= 0 \\ x^2 &= -25 \\ x &= \pm\sqrt{-25} \end{aligned}$$

$\boxed{x = \pm 5i}$
COMPLEX

28) $f(x) = x^3 + 13x^2 + 57x + 85$ Three Zeros Real at $x = -5$

$$\begin{array}{r|rrrr} -5 & 1 & 13 & 57 & 85 \\ & & -5 & -40 & -85 \\ \hline & 1 & 8 & 17 & 0 \end{array}$$

$x^2 + 8x + 17$ CANNOT BE FACTORED

$$\frac{-8 \pm \sqrt{8^2 - 4(17)}}{2} = \frac{-8 \pm \sqrt{64 - 68}}{2}$$

$$\frac{-8 \pm \sqrt{-4}}{2} = \frac{-8 \pm 2i}{2} = -4 \pm i$$

REAL ZERO: $\boxed{x = -5}$
 COMPLEX ZEROS: $\boxed{x = -4+i, x = -4-i}$

32) $f(x) = x^4 + 3x^3 - 19x^2 + 27x - 252$ 4 ZEROS
 REAL $\boxed{x = -7, x = 4}$ $(x-4)(x+7) = x^2 + 3x - 28$

$$\begin{array}{r} x^2+9 \\ x^2+3x-28 \quad \begin{array}{l} x^4+3x^3-19x^2+27x-252 \\ -x^4+3x^3-28x^2 \\ \hline 9x^2+27x-252 \\ -9x^2+27x-252 \\ \hline 0 \end{array} \end{array}$$

$$\begin{aligned} x^2+9 &= 0 \\ x^2 &= -9 \end{aligned}$$

$$\begin{aligned} x &= \pm\sqrt{-9} \\ \boxed{x = \pm 3i} \\ \text{COMPLEX} \end{aligned}$$